# The flux growth of rare earth germanomolybdates and germanotungstates

S. J. SWITHENBY, B. M. WANKLYN, M. R. WELLS The Clarendon Laboratory, University of Oxford, UK

The growth of  $R_2GeMoO_8$  and  $R_2GeWO_8$  crystals from the flux systems  $R_2O_3$ -GeO<sub>2</sub>-MO<sub>3</sub>-PbO, where M = Mo or W, is described. A preliminary investigation of their magnetic properties is reported. The X-ray powder pattern data for  $R_2GeWO_8$  with R = Gd, Tb, Dy, Ho and Er are given.

# 1. Introduction

The compounds  $R_2GeMoO_8$  have the CaWO<sub>4</sub> (scheelite) structure, space group I4<sub>1</sub>/a, with the smaller cation sites randomly occupied by tetravalent Ge and hexavalent Mo respectively [1]. The interest in these materials arises from the fact that the rare earth ions are sufficiently concentrated for magnetic transitions in the liquid helium temperature range to be expected.

The analogous compounds  $RNaMo_2O_8$  and  $RLiMo_2O_8$ , which also have the scheelite structure but are magnetically more dilute, have been reported [2, 3]. The latter occurs as an epitaxial layer on  $R_2GeMoO_8$  crystals grown from lithium ditungstate flux [4], and the possibility of some degree of solid solution of the two compounds cannot be excluded. It was decided to attempt to use a flux system less likely to contaminate the crystals, and to discover whether the magnetically concentrated analogues,  $R_2GeWO_8$ , could be prepared.

This paper reports the growth of the compounds  $R_2GeMoO_8$  and  $R_2GeWO_8$  where R =Gd, Tb, Dy, Ho and Er, and preliminary investigations of their magnetic properties. The four-component system  $R_2O_3$ -GeO<sub>2</sub>-MO<sub>3</sub>-PbO (M = Mo or W) has several advantages.

1. One of the authors had already grown  $R_2Ge_2O_7$  from PbO- $R_2O_3$ -GeO<sub>2</sub> [5] and  $R_2MoO_6$  from PbO- $R_2O_3$ -MoO<sub>3</sub> [6] and it seemed likely that  $R_2GeMoO_8$  would crystallize from the combination of these systems.

2. The presence of three ions common to both crystal and flux greatly reduces the incorporation of impurities in the former.

3. Pb<sup>2+</sup> usually replaces the smaller rare earth ions to the extent of only 0.02 to 0.3 %.

4. The combined flux would probably be of low volatility.

## 2. Equipment

The furnaces, control equipment and flux growth technique have been described previously [7]. The crucibles were of 20 or 50 cm<sup>3</sup> capacity and of pure platinum of 0.50 mm wall thickness. Each was provided with a tightly fitting lid.

The chemicals used were: Rare Earth Products 99.9% pure  $R_2O_3$ , BDH "Analar" MoO<sub>3</sub>, PbO and PbO<sub>2</sub>, and "Laboratory Reagent" WO<sub>3</sub> and GeO<sub>2</sub>.

## 3. Crystal growth

In crystal growth from a four-component system, it is essential to reduce the number of variables to a minimum and this was achieved as follows:

1. The solubility of rare-earth complex oxides in PbO-based fluxes at 1260 to 1300°C is typically 3 to 5 wt %  $R_2O_3$  (e.g. with RVO<sub>4</sub> from Pb<sub>2</sub>V<sub>2</sub>O<sub>7</sub> [8],  $R_2Ge_2O_7$  and  $R_2GeO_5$  from PbO-GeO<sub>2</sub> [5],  $R_2MOO_6$  from PbO-MoO<sub>3</sub> [6], RPO<sub>4</sub> from Pb<sub>2</sub>P<sub>2</sub>O<sub>7</sub> [9]) and a solubility of this order was assumed.

2. In the PbO-GeO<sub>2</sub> system, the liquidus falls steeply with small additions of GeO<sub>2</sub> to PbO [10]. The liquidus temperature was accordingly reduced by adding more GeO<sub>2</sub> than is required for the formula  $R_2GeMoO_8$ , and an  $R_2O_3$ :GeO<sub>2</sub> ratio near 1: 3 (molar) was used.

These assumptions were justified by the

© 1974 Chapman and Hall Ltd.

Components	Crucible volume (cm³)	Maximum temperature and holding time	Cooling programme	Results
1.8 g Gd <sub>2</sub> O <sub>3</sub> , 1.5 g GeO <sub>2</sub> , 27.7 g PbO, 9 g MoO <sub>3</sub> , 2.2 g PbO <sub>2</sub>	20	1290°C (24 h)	2°C h <sup>-1</sup> to 1240°C 3°C h <sup>-1</sup> to 900°C	Clear, well- formed crystals
1.4 g Gd <sub>2</sub> O <sub>3</sub> , 2.2 g GeO <sub>2</sub> , 20 g PbO, 14 g WO <sub>3</sub> , 2.4 g PbO <sub>2</sub>	20	1280°C (10 h)	4° C h <sup>-1</sup> to 900° C	Clear crystals shown in Fig. 2

TABLE I Starting compositions and flux growth conditions

appearance of crystals up to 2 mm in length after only four trial experiments.

3. In attempts to produce  $R_2GeWO_8$ , similar considerations were applied with comparable results.

The crucibles were supported in groups of four in Morgan M1 3000 refractory brick. Each crucible was placed in a hollow in the brick, with alumina powder packed around it, and a slab of brick was placed over the top to protect the furnace from attack by PbO vapour and provide additional thermal insulation.

## 4. Results

#### 4.1. R<sub>2</sub>GeMoO<sub>8</sub>

It was found that with PbO:MoO<sub>3</sub> = 2.4:1 or greater, and R<sub>2</sub>O<sub>3</sub>:GeO<sub>2</sub> as described above, rare earth germanates crystallized. At borderline compositions, the ionic radii of the rare earths were found to determine the phase obtained. With PbO:MoO<sub>3</sub> = 2.4:1, and the other molar proportions the same, with Tb<sub>4</sub>O<sub>7</sub> in one batch and Ho<sub>2</sub>O<sub>3</sub> in the other, the respective products were Tb<sub>2</sub>GeMoO<sub>8</sub> and (Ho<sub>2</sub>Ge<sub>2</sub>O<sub>7</sub> + Ho<sub>2</sub>GeO<sub>5</sub>).

Table I gives the composition and growth conditions which produced the best crystals of  $Gd_2GeMoO_8$ . The loss in weight was usually less than 3 wt %.

A slow rate of cooling (2 to  $4^{\circ}C^{-1}$ ) produced clear, well-formed crystals, even with only 20 cm<sup>3</sup> crucibles. Cooling at faster rates resulted in skeletal forms, platelets or dendrites.

The well-formed crystals were bipyramids with the characteristic colours of the trivalent rare earth ions. The germanomolybdates were dull in appearance even when the crystals were clear and free from flux inclusions. Microscopic examination showed this to be due to rough surfaces on the facets, which were sometimes scaly or corrugated.

The X-ray powder patterns for  $R_2GeMoO_8$ agreed closely with published data [1]. EPMA showed that the lead content of  $Tb_2GeMoO_8$ was  $0.25\frac{1}{6}$ .

#### 4.2. R<sub>2</sub>GeWO<sub>8</sub>

Table I gives the composition and growth conditions which produced the best crystals of  $Gd_2GeWO_8$ . The crystals grown from the system  $Gd_2O_3$ -GeO<sub>2</sub>-WO<sub>3</sub>-PbO had the same habit as  $R_2GeMoO_8$ . Their powder patterns



Figure 1 Unit cell parameters of  $R_2$ GeWO<sub>8</sub> plotted versus lanthanide atomic number:  $+: a_0, 0: c_0$ .

hkl	Intensity (estimated)	dobs					
	(estimated)	Er <sub>2</sub> GeWO <sub>8</sub>	Ho <sub>2</sub> GeWO <sub>8</sub>	Dy <sub>2</sub> GeWO <sub>8</sub>	Tb <sub>2</sub> GeWO <sub>8</sub>	Gd <sub>2</sub> GeWO <sub>8</sub>	
101	M	3.38		3.32	3.35	3.37	
112	VS	2.99	3.01	3.01	3.02	3.04	
004	MS	2.74	2.77	2.77	2.92	2.80	
200	S	2.52	2.54	2.54	2.55	2.56	
121	М	2.21		2.22	2.24	2.25	
114	W	2.18		2.20	2.20	2.22	
105	W	2.02				2.05	
123	W	1.92				1.95	
204	VS	1.860	1.870	1.872	1.878	1.887	
220	MS	1.785	1.795	1.794	1.800	1.811	
301	VW	1.659		1.668	1.675	1.684	
116	S	1.630	1.639	1.643	1.650	1.661	
132	VS	1.532	1.542	1.542	1.547	1.554	
107	MS	1.498	1.506	1.508	1.513	1.519	
008	VW	1.373	1.383	1.386	1.393	1.402	
400	W	1.263	1.268	1.270	1.275	1.279	
136	S	1.205	1.213	1.214	1.220	1.225	
413	М	1.164	1.171	1.171	1.175	1.180	
404	MW	1.148	1.155	1.155	1.160	1.164	
420	MW	1.131	1.137	1.138	1.140	1.145	
		a <sub>0</sub> 5.06 Å	a <sub>0</sub> 5.08 Å	a <sub>0</sub> 5.09 Å	<i>a</i> <sub>0</sub> 5.10 Å	a <sub>0</sub> 5.12 Å	
		c <sub>0</sub> 11.00 Å	c₀ 11.06 Å	с <sub>0</sub> 11.09 Å	c <sub>0</sub> 11.15 Å	c₀ 11.20 Å	

TABLE II X-ray powder pattern data for the compounds R<sub>2</sub>GeWO<sub>8</sub>

corresponded closely to those of  $R_2GeMoO_8$  and have been similarly indexed. Table II gives the X-ray powder pattern data and unit cell parameters for the compounds  $R_2GeWO_8$ , and in Fig. 1 the latter are plotted versus ionic radii of the rare earth ions.

A mixture of composition  $(Gd_2O_3 + GeO_2 + WO_3)$  was sintered by heating it in a Pt crucible for 6 h at 1250°C. The X-ray powder pattern of the product corresponded to that of the crystals and confirmed the formula  $Gd_2GeWO_8$ . With  $R_2GeWO_8$ , it was found possible to use relatively more  $GeO_2$  and less  $WO_3$  (as molar percentages) in this system without rare earth tungstates being produced.

The germanotungstates were shiny, the surfaces vitreous in appearance and somewhat curved (Fig. 2).

# 5. Magnetic susceptibility measurements

Measurements of the magnetic susceptibility of small quantities of the compounds have been made in the temperature range 0.5 to 4.2 K. In each case the sample consisted of many small



Figure 2 Crystals of  $Gd_2GeWO_8$  (1 mm  $\times$  2 mm grid).

crystallites, of typical mass 0.05 g, so that the data are representative of "powder" susceptibilities. The measurements were made by two methods; an a.c. (175 Hz) mutual inductance technique [11] and a d.c. low field (less than 1 kOe) method described by Cashion *et al.* [12].

R	R <sub>2</sub> GeWO <sub>8</sub>				R <sub>2</sub> GeMoO <sub>8</sub>		
	C	θ	gcalc	g theoretical	C	θ	gcalc
Ть	9.4	2.0	17.3	18	12.0	2.3	19.6
Dy	12.8	2.7	20.2	20	12.3	2.5	19.8
Ho	11.2	1.8	18.9	20	12.4	2.1	19.9
Er	7.7	1.6	15.7	18	7.9	1.8	15.9

TABLE III The experimental values of the Curie constant C (cgs units) and Weiss  $\theta$  (K) together with the experimental and theoretical g-values.

The results have been analysed and, with the exception of the two gadolinium compounds, fitted to the simple Curie-Weiss law relationship

$$\chi = \frac{C}{T+\theta} \cdot$$

The validity of such an analysis and the definition of the parameters have been given in a previous paper [13].  $Gd_2GeMoO_8$  and  $Gd_2GeWO_8$  are not amenable to such a treatment as magnetic ordering occurs at approximately 1.4 K and the Curie-Weiss law is strictly only valid at temperatures well above the ordering temperature. Table III gives the measured values of the parameters C and  $\theta$  and it should be noted that the susceptibility  $\chi$  refers to the molar susceptibility per rare earth ion.

From the measured values of the Curie constant it is possible to obtain an estimate of the g-value associated with the rare earth ion. If we assume that the only occupied energy level is doubly degenerate (an assumption that is strictly valid for the Kramers ions Dy and Er) then the Curie constant is equal to  $Ng^2\beta^2/4k$ . For a powder susceptibility measurement a mean square g-value is obtained but if we consider that this arises from a single uniaxial g-value then we obtain the value denoted by  $g_c$ . This may be compared with the maximum theoretical value  $g_t$ , which is calculated on the assumption that the effect of the crystalline electric field is to split the free ion ground state such that the lowest level is a doublet with the maximum value of  $M_{\rm J}$ . The results given in Table III show that our experimental results are compatible with the theoretical g-values calculated using the assumptions stated above.

For the Ho, Er and Tb compounds of each series the measurements were made down to 1 K; in each case there was no indication of any magnetic ordering occurring. The behaviour of



Figure 3 The reciprocal susceptibility versus temperature of the gadolinium and dysprosium compounds; (a)  $Gd_2GeWO_8$ , (b)  $Gd_2GeMoO_8$ , (c)  $Dy_2GeWO_8$ , (d)  $Dy_2GeMoO_8$ .

the Gd and Dy compounds is shown in Fig. 3, where the reciprocal susceptibility per ion is plotted as a function of temperature. For  $Dy_2GeWO_8$  (curve c) and  $Dy_2GeMOO_8$  (curve d) the measurements were extended to the lowest temperature as there is clearly a departure from the Curie-Weiss law behaviour. At approximately 1 K for both compounds, the magnetic susceptibility becomes almost temperature independent indicating that some form of cooperative phenomenon is present. It is not possible to state the precise nature of the process although an antiferromagnetic state seems likely. The environment of the rare earth ion in these compounds is not unique, being subject to the random occupation of the smaller cation site. This situation may result in local ordering of the rare earth ions with a corresponding broad peak in the susceptibility curve at the average transition temperature.

In  $Gd_2GeWO_8$  (curve a) and  $Gd_2GeMoO_8$ (curve b) the onset of magnetic ordering occurs at 1.5 and 1.4 K respectively. For the  $Gd^{3+}$  ion, which has an isotropic *g*-value, it is to be expected that after ordering to an antiferromagnetic state the powder susceptibility will decrease below the Néel point to a value which is  $\frac{2}{3}$  of the susceptibility at the Néel temperature. This clearly does not happen in either of these two compounds. We speculate that this may be due to the random environment of the rare earth ions as with the dysprosium compounds.

# 6. Conclusion

A method has been described which produces good quality crystals of  $R_2GeMoO_8$  and  $R_2GeWO_8$ . The flux system used is relatively non-volatile and it should be possible for larger crystals to be grown by top seeding. If a more adequate explanation of the magnetic behaviour is to be achieved then further experiments at low temperatures are necessary. However, the random occupation of the smaller cation site may well preclude a complete understanding.

## Acknowledgements

The authors are grateful to Dr S. H. Smith for technical assistance, to Mr F. Wondre for providing the X-ray powder pattern data, and to Mr W. Davison of the School of Physics, University of Newcastle upon Tyne, for EPMA. This work was supported in part by the Science Research Council and one of the authors (S.J.S.) wishes to acknowledge the support of an SRC grant.

#### References

- 1. C. B. FINCH, L. A. HARRIS and G. WAYNE CLARK, Proc. Fourth Conf. on Rare Earth Res., April 1964 (Gordon and Breach, New York, 1965).
- 2. M. SCHIEBER and L. HOLMES, J. Appl. Phys. 35 (1964) 1004.
- 3. L. G. VAN UITERT and R. R. SODEN, *ibid* **31** (1960) 328.
- 4. G.W. CLARK, C. B. FINCH, L. A. HARRIS and H. L. YAKEL, J. Crystal Growth 16 (1972) 110.
- 5. B. M. WANKLYN, J. Mater. Sci. 8 (1973) 649.
- 6. Idem, to be published.
- 7. G. GARTON, S. H. SMITH and B. M. WANKLYN, J. Crystal Growth 13/14 (1972) 588.
- 8. G. GARTON and B. M. WANKLYN, Colloques Internationaux du CNRS No. 180, Les Elements des Terres Rare 1 (1969) 343.
- 9. B. M. WANKLYN, J. Mater. Sci. 7 (1972) 813.
- 10. B. PHILLIPS and M. G. SCROGER, J. Amer. Ceram. Soc. 48 (1965) 399.
- 11. F. R. MCKIM and W. P. WOLF, J. Sci. Instrum. 34 (1957) 64.
- 12. J. D. CASHION, A. H. COOKE, T. L. THORP and M.R.WELLS, *Proc. Roy. Soc.* (Lond.) A 318 (1970) 473.
- 13. J. D. CASHION, A. H. COOKE, M. J. M. LEASK, T. L. THORP and M. R. WELLS, J. Mater. Sci. 3 (1968) 402.

Received 8 October and accepted 22 October 1973.